

Slick Packets

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Abstract

Source-controlled routing has been proposed as a way to improve flexibility of future network architectures, as well as simplifying the data plane. However, if a packet specifies its path, this precludes fast local re-routing within the network. We propose SLICKPACKETS, a novel solution that allows packets to slip around failures by specifying alternate paths in their headers, in the form of compactly-encoded directed acyclic graphs. We show that this can be accomplished with reasonably small packet headers for real network topologies, and results in responsiveness to failures that is competitive with past approaches that require much more state within the network. Our approach thus enables fast failure response while preserving the benefits of source-controlled routing.

1. INTRODUCTION

Traditional routing protocols are **network-controlled**: routes are computed within the network, with each router picking, from among its neighbors, the next-hop to each destination. Examples include BGP for interdomain routing, and OSPF for intradomain routing. An alternate paradigm, **source-controlled routing** (SCR), improves the flexibility of the network architecture. Rather than computing all routes within the network, SCR architectures [10, 20, 28–30] reserve some choice of routes for the *sources*¹ to select on a per-packet basis. The uses of SCR’s routing flexibility are quite diverse. Sources can observe end-to-end reliability problems and switch to a working path within a few round-trip times (RTTs); pick better-performing routes based on observed performance [5, 11, 24]; improve load balance since path selection is finer-grained [23]; encourage competition among network providers [7]; improve security [27]; or optimize for other application-specific objectives. SCR is thus a promising approach to improve the flexibility of the network layer in future Internet architectures.

However, one remaining problem is that of *fast failure reaction*. This problem arose in early network-controlled routing (NCR) protocols, which suffered from unreliability during network dynamics: during the distributed

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¹In this paper, we use “source” to refer either to end-hosts or to edge routers acting on their behalf.

convergence process, packets could enter “black holes” or loops, resulting in tens of seconds or minutes of downtime in Internet end-to-end paths [14, 26]. Treating these basic protocols as a baseline, two high-level approaches have been proposed to improve failure reaction.

The first approach works within the NCR paradigm by computing an alternate path to each destination (or IP prefix or AS); a router can locally switch to the alternate path without waiting for a control-plane convergence process. Packets can thus be delivered continuously, except for the minimal time it takes for a router to detect failure of one of its directly connected links and locally switch to an alternate path. Examples include MPLS Fast Reroute [22], SafeGuard [18], and FCP [17] for intradomain routing, and R-BGP [16] for interdomain routing. However, this approach lacks the routing flexibility of SCR.

A second approach to improve failure reaction is to leverage SCR’s routing flexibility: a source can switch routes without waiting for the Internet’s control plane to reconverge. While this improves failure reaction time relative to the baseline above, the source still must wait to receive notice of the failure. Regardless of the means of notification, this will take at least on the order of one RTT, which at Internet scales would be much slower than the first approach of using NCR with alternate paths. And in the SCR proposals that provide the most flexibility [10, 29], sources specify in the packet header an explicit route (perhaps at the level of autonomous systems) rather than a destination, so the NCR and SCR techniques cannot be immediately combined.

The goal of this paper is to achieve the best of two worlds: the fast failure reaction of alternate routes embedded within the network, and the flexibility of routes chosen by sources at the edge of the network. To meet this goal, we work within the SCR paradigm, but with a twist. Instead of specifying a single path to the destination, the packet header contains a directed acyclic graph that we call the *forwarding subgraph* (FS). Each router along the packet’s path may choose to forward it along any of the outgoing links at that router’s node in the FS (optionally preferring a path marked as the primary), with no danger of causing a forwarding loop. This approach, which we call SLICKPACKETS, allows packets to “slip” around failures in-flight while retaining the flexibility of source route control. Moreover, SLICKPACKETS pro-

vides a scalability benefit over NCR with alternate paths: rather than requiring multiple routes to every destination in every router's forwarding table, SLICKPACKETS routers need only local information.

Of course, our approach also presents several challenges. Chief among these is how to encode an FS with sufficient path diversity into the small space afforded by a packet header. We introduce techniques through which the FS can be encoded compactly enough for our mechanism to be feasible. For example, an FS providing an alternate path at every hop along the primary occupies less than 26 bytes for 99% of evaluated source-destination pairs in an AS-level Internet map, and no higher than 50 bytes in all evaluated cases. Thus, the technique incurs manageable overhead for applications that send packets of moderate to large size. We also demonstrate through a simulation-based performance evaluation that SLICKPACKETS achieves failure reaction performance that is comparable to the best of NCR architectures [18].

The rest of this paper proceeds as follows. In §2, we present an overview of SLICKPACKETS and its principal design challenges. §3 gives a detailed presentation of the SLICKPACKETS design. We evaluate the performance of our design in terms of header size and failure reaction in §4. We discuss extensions of SLICKPACKETS in §5 and related work in §6, and conclude in §7.

2. OVERVIEW

In this section, we provide an overview of SLICKPACKETS, and discuss several critical design challenges.

SLICKPACKETS is a failure reaction mechanism for SCR protocols. In contrast to traditional SCR protocols that specify a single path in the packet header, SLICKPACKETS enables fast recovery within the network by allowing the source to embed the rerouting information within the packet header in the form of a **forwarding subgraph (FS)**. The FS specifies a set of paths that intermediate routers can use to reroute packets in case of failures. The source, if it desires, can designate one of these paths as the **primary path** to be used in the absence of failure; the rest of the paths are then treated as **alternate paths** that can be used if the primary path is not available. In order to avoid forwarding loops, SLICKPACKETS requires that the FS be a directed acyclic graph (DAG).

Performing forwarding in this way has two main benefits. First, since the source specifies the FS, it has full control of not only the primary path, but also how the network forwards the packet when the primary path is not available. Second, since alternate path information is embedded directly in the packet header, the network can react immediately without requiring involvement of the source, which reduces the reaction time in presence of link failures. In addition to these two benefits, the task of a router becomes simpler: a router requires only local knowledge of its neighbors, rather than needing an alternate path for every destination (which may require information such as the multi-homing locations of each host). In summary, SLICKPACKETS achieves key benefits of SCR architectures (flexibility in route selection and scalability of network routing state) while simultaneously attaining failure reaction performance that is comparable to that of NCR architectures with backup paths.

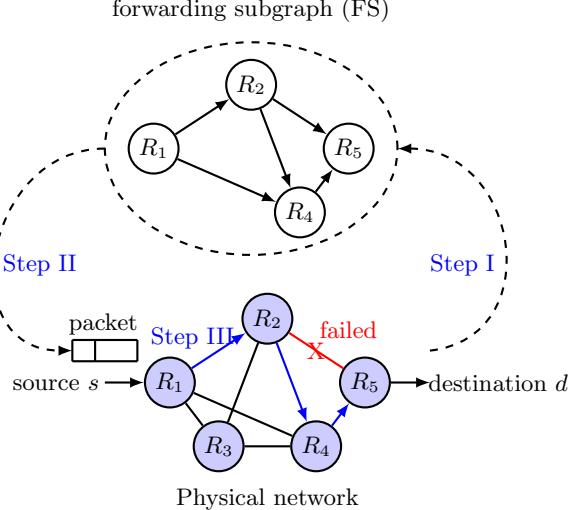


Figure 1: Overview of the SLICKPACKETS design. Step I: the source selects a **forwarding subgraph (FS)** based on the topology of the physical network; Step II: the source encodes and embeds the FS in the packet header to inform routers how to route around encountered failures; and Step III: routers forward the packet based on the FS contained in the packet header.

Fig. 1 shows an example to illustrate the design of SLICKPACKETS. Suppose the source s wishes to send a packet to a destination d . The source has acquired, by some mechanism to be discussed later, a map of the network. It selects the FS as shown in Fig. 1 and designates (s, R_1, R_2, R_5, d) to be the primary path. Note that the FS provides each node on the primary path with sufficient alternatives so that if a link on the primary path fails, the packet can be rerouted to the destination. Next, s constructs a data packet with the subgraph embedded in the packet header, and forwards it on to the first-hop R_1 . At R_1 , the packet is forwarded to the next-hop on the primary path (R_2). Now suppose that at R_2 the primary path's next hop R_5 lies across a failed link (R_2, R_5); then R_2 forwards the packet to R_4 , the next-hop on its alternate path in the FS, after which the packet continues to R_5 and finally d .

Realizing the high level idea of source-controlled routing along an FS, however, involves several key challenges. We outline these challenges and our solutions here.

Obtaining the map. Like other SCR architectures in which sources construct end-to-end paths, our sources require a map of the available links. When deploying SLICKPACKETS as an interdomain routing protocol, this immediately raises questions of scalability and policy compliance. Is it feasible to push a map of the Internet, at some level of granularity, to every source or at least every edge router? Is there an acceptable way to balance control of network resources between the senders and the network owners? Fortunately, we can adopt the solutions developed by past work, in particular NIRA [29] and pathlet routing [10], which have shown how maps of policy-compliant transit service can be constructed and disseminated.

inated in ways that can be much *more* scalable than traditional NCR protocols like BGP.

Packet header overhead. The next challenge is to design an efficient encoding mechanism that embeds the FS into the packet header with minimal overhead. By using link labels with only local significance and allocating every bit carefully, we are able to achieve acceptable packet header sizes on realistic network topologies.

Fast data-plane operations. Another challenge is to design an efficient data plane forwarding algorithm: the encoding and forwarding mechanisms in SLICKPACKETS should minimize next-hop lookup time without substantially increasing header processing cost, forwarding delay and/or design complexity of modern router forwarding planes. Fortunately, forwarding along an FS requires only lookup and pointer-increment operations, as in standard SCR protocols, and can be efficiently implemented in practice.

The next section discusses our design in more detail, including our solutions to these challenges.

3. SLICKPACKETS DESIGN

In this section, we present in more detail the four main components of SLICKPACKETS: definition and dissemination of the network map (§3.1); selection of a forwarding subgraph (FS) at the source (§3.2); encoding of the FS into the packet header (§3.3); and the data plane forwarding mechanism at routers (§3.4).

The SLICKPACKETS approach could be applied in multiple contexts. We describe here how the design can be applied to interdomain and intradomain routing. The differences principally lie in map dissemination and data plane forwarding, with the core approach taking the same form in both contexts.

3.1 Map format and dissemination

As in other SCR protocols in which the source composes end-to-end paths [10, 29], in SLICKPACKETS, the source must obtain a network “map” (topology) from which it can construct paths. This map is an abstract directed graph in which each directed directed link (u, v) at node node u is annotated with a *label*. The label is a compact, variable-length bitstring, which the source will use when encoding the FS (§ 3.3) to tell node u that it wants u to use the link (u, v) . Similar to an MPLS label, the label identifies a link only locally at u , not globally. Thus, u will generally announce labels of length $\lceil \log_2 \delta(u) \rceil$ bits where $\delta(u)$ is the degree of u .

What this map corresponds to in the physical network and how the map is disseminated depend on the deployment scenario. In an intradomain environment, the map would correspond to the physical topology of routers and links and could be distributed via a protocol like OSPF or through a centralized coordinator as in [17].

In an interdomain environment, we have to deal with the significant challenges of scalability and network owners’ transit policies. In order to overcome these challenges, we build on solutions developed in past work and briefly describe them here for completeness.

Basic approach. Both NIRA [29] and pathlet routing [10] provide sources with a policy-compliant map of the Internet, roughly at the autonomous system (AS)

level. NIRA’s map assumes common customer-provider-peer relationships between ASes and allows a subset of *valley-free* routes: that is, packets travel up a chain of providers, potentially across a peering link, and down a chain of customers to the destination. Pathlet routing represents this map explicitly as an arbitrary virtual topology, whose edges (pathlets) represent policy-compliant transit service.

Scalability. NIRA, while dependent on the existence of a typical AS business hierarchy, offers the opportunity of vastly *improving* BGP’s control plane scalability. Rather than learning an Internet-wide topology, each node learns its “up-graph” of routes through providers, stopping at the “core” of the Internet. The up-graph requires fewer than 20 entries for 90% of domains [29], many orders of magnitude less than the roughly 300,000 prefixes that BGP propagates today. Each destination stores its up-graph in a global DNS-like database; to route to a destination, a source queries the database and combines its own up-graph with the destination’s up-graph. Though the resulting map is a small fraction of the Internet, it includes all policy-compliant (valley-free) routes. Pathlet routing could use a NIRA-style approach for disseminating the pathlet topology, or it can be disseminated via a BGP-like mechanism with slightly more messaging and control state ($\leq 1.7\times$) than traditional BGP.

SLICKPACKETS can take advantage of either the pathlet or NIRA approach for interdomain map dissemination. Thus, SLICKPACKETS does not require a source to have complete topological knowledge of the network, but rather only enough to construct a path and alternate paths to the destination.

We also note that SLICKPACKETS, like other SCR and multipath routing architectures, can benefit from significantly reduced rate of control plane updates [6] compared with basic single-path NCR architectures. This is because short-lived failures need not be disseminated through the control plane, since failure reaction will happen anyway via forwarding along alternate paths without waiting for control-plane updates.

Link labels. Along with the map itself, SLICKPACKETS requires labels on the links. Routers (or ASes for interdomain; for convenience we’ll use “routers” in what follows) can piggyback this information with the link advertisements [10]. To change a label, a router readvertises the link. While readvertisements increase control traffic, we expect that changing a router’s link labels will be fairly rare, for two reasons. First, the operator could change a single label from one bit sequence to another; however, there should be little need for such changes because the labels are arbitrary identifiers with no significance. Second, the operator may need to increase the number of links exiting the router. This *may* increase the label length and require readvertisements of all of the router’s link labels, creating a period of inconsistency from when the router changes its label length to when sources receive the updated announcement. However, label lengths change only once every time the number of outgoing links doubles (or halves) in size, which is expected to be a very rare event.

An alternate approach is to make labels self-describing: their first few bits encode the label length [10]. This avoids the need to readvertise links after a length change

and the resulting inconsistency, but labels become slightly longer. Since compactness is important for SLICKPACKETS, we do not evaluate this approach in this paper.

Map consistency. A natural question is whether all sources and the network must have an entirely consistent view of the map at all times. Fortunately, this difficult task is unnecessary. There are three possible types of inconsistency.

First, if a source uses a non-existent label (e.g., the link has been removed or its label changed), this is equivalent to a link failure and the packet can be re-routed along an alternate path. To avoid even this minor disturbance, routers can insert a short delay between announcing a label deletion and its removal from forwarding tables.

Second, if a source uses a label that has changed to identify a different link, then the packet will follow an incorrect path and will be unlikely to reach its intended destination. This is similar to inconsistency problems in basic NCR protocols. (Unlike in basic NCR protocols, however, the packet cannot get into a loop of any significant length because one link in the DAG will be consumed at each hop.) To avoid label-change inconsistency, routers can simply use new labels rather than reusing ones that have recently had a different meaning.

Third, a source might be unaware of some valid labels. This simply results in a slightly restricted set of options until it receives the relevant control plane advertisement, as in essentially any other distributed routing protocol.

Thus, in all cases, inconsistency issues can be mitigated.

3.2 Selection of the forwarding subgraph

Once a source has obtained the network map, it selects a *forwarding subgraph* (FS) along which it desires the packet to be routed in the network. The FS is a DAG corresponding to a subset of nodes and links in the network map. The directed edges inform routers of the packet’s allowed next-hops, and acyclicity ensures there are no forwarding loops. Additionally, for each node in the FS, the source may mark one outgoing link as the preferred primary.

Sources have a great deal of flexibility in how they choose an FS. For instance, the source may select an FS that avoids any single link failure along a low-latency primary path, avoids node failures, optimizes for other metrics like bandwidth, or picks alternate paths that avoid shared risk link groups. We discuss some of these uses in §5. For concreteness, we describe here and evaluate in §4 how the source can pick an FS that will minimize primary-path latency and provide alternate paths to avoid any single link failure. As noted below, accommodating shared risk link groups is similar.

A source s , for a given destination d , constructs a single-failure-avoiding FS as follows. First, s computes a primary path P to d by running a shortest path algorithm over the network map. Next, s visits each link along P , and computes the alternate path P_i it would prefer the packet to be routed along if that link were to fail. In particular, for each node v_i on the primary path, we (a) remove v_i ’s outgoing edge corresponding to its next hop along the primary path; (b) compute a shortest path from v_i to d , not using the removed outgoing edge; and (c) restore the removed edge. In case of a node having multiple shortest paths to the destination, the source may arbitrarily

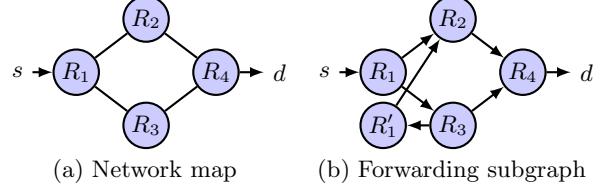


Figure 2: An FS may have multiple representations of a network map node, to allow “backtracking” without introducing cycles in the FS.

select one of these shortest paths. Finally, the primary and the alternate paths are assembled into the FS. Note that the above algorithm requires $|P|$ runs of Dijkstra’s algorithm. Surprisingly, it is possible to construct a primary path and all the alternate paths in a *single* run of a shortest-path algorithm; see [12].

Beyond single-link-failure protection, a source may want to protect against failures of shared risk link groups (i.e., sets of links that are likely to have correlated failures, such as multiple logical links allocated to a single physical fiber). Assuming it has knowledge of these groups, it can do this by removing all links in the group in substep (a) above, and restoring them all in (c).

Note that there is a subtlety in how the the primary and the alternate paths are “assembled” into the FS: if we simply take the union of all these links and edges, we might create a loop, violating the acyclicity requirement. Consider the network map in Fig. 2(a). Assume that s desires to use (s, R_1, R_3, R_4, d) as the primary path. Then to escape a failure of the link (R_3, R_4) , a packet located at R_3 must follow the path (R_3, R_1, R_2, R_4, d) . Taking the union of these primary and alternate paths would result in a loop $R_1 \rightarrow R_3 \rightarrow R_1$. Due to symmetry, the problem persists if (s, R_1, R_2, R_4, d) is the primary path.

In order to avoid such loops, when adding an alternate path edge (u, v) to the FS, we first check to see if this would cause a loop. If so, we create a second FS representation v' of the physical node v , and add the edge (u, v') . This can be seen as “tunneling” the packet back along an alternate path. In the example of Fig. 2, before adding the second alternate path, we create a new copy R'_1 corresponding to the node R_1 . The alternate path then follows (R_3, R'_1, R_2, R_4, d) , resulting in a acyclic representation of the FS as shown in Fig. 2(b).

3.3 Encoding the forwarding subgraph

After choosing an FS, the source must encode the FS into a sequence of bits and place it in the packet header. SLICKPACKETS is agnostic to the particular location this header appears in the packet (for example, it may reside in a “shim” header between the IP and MAC layers, in an IP option, or in a novel header format in a next-generation Internet protocol). There are two key goals in designing an encoding format: (a) minimizing the size of the resulting encoding; and (b) ensuring data plane forwarding operations are simple. We designed and evaluated several encoding formats to achieve these goals.

In this paper we present two encoding formats, called Direct and Default. Each may result in a smaller encoding in certain scenarios as discussed below. But the latter re-

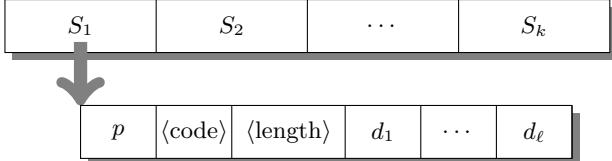


Figure 3: Default encoding format layout. S_i is the segment corresponding to node v_i on the primary path. It encodes the node’s primary next hop p and alternate path $(d_1, d_2, \dots, d_\ell)$. $\langle \text{length} \rangle$ specifies the bit-length of the alternate path, and $\langle \text{code} \rangle$ specifies the bit-length of the $\langle \text{length} \rangle$ field.

sulted in smaller encoding sizes in the network topologies we evaluated using the single-failure-avoiding FS selection (§3.2), so it is our default.

Direct format. The Direct format encodes the FS directly, in the sense that the FS’s DAG data structure in memory is essentially directly serialized into a DAG data structure in the packet header. The header contains a sequence of node representations, each containing one or more outgoing link representations; each link representation contains its corresponding label and a pointer to another node within the header, corresponding to the node at the other end of the link. We describe the bit-layout of this format in detail in Appendix B.

Default format. One source of overhead in the Direct format is the use of pointers within the header. Our Default format avoids some of that overhead, by grouping together sequences of labels corresponding to alternate paths, without needing an explicit representation of each node along the alternate path. The disadvantage of this grouping is that it involves duplicating link representations, similar to how a depth-first traversal of all paths in the DAG could visit links multiple times.

In fact, there exist DAGs that have exponentially large numbers of possible traversals (thus specifying exponentially large numbers of ways the packet could be forwarded through the network). Consequently, the Direct format can be exponentially more efficient than the approach of Default in the most extreme case. In general, we expect Direct will be more compact for situations in which the alternate paths often share nodes with one another or with the primary. However, in this paper we focus on the particular application of choosing single-failure-avoiding FSes. For that application, we found that the savings from avoiding pointers outweighed the duplication of link representations, so that Default was somewhat more compact in several realistic networks (§4). We therefore choose the Default format as our default and describe it in more detail now.

In the Default format, the FS is represented as a sequence of **segments**, one for each router on the primary path. For instance, in Fig. 3, the primary path consists of k hops and S_1, S_2, \dots, S_k are the segments corresponding to those k hops. The segment corresponding to a router v on the primary path contains three pieces of information (see Fig. 3): (a) v ’s next-hop on the primary path; (b) the bit-length of the encoding of v ’s alternate path; and (c) v ’s alternate path, as a sequence of next-hop labels. By “ v ’s alternate path” we mean the alternate path begin-

ning at v that avoids the primary next-hop from v . (We assume here that the FS has the format of one alternate path for each link on the primary.²)

For (a), we need to include the router’s label (§3.1) for the given outgoing edge, and similarly for (c) we include a sequence of labels. Recall that these labels are only locally unique to each node, which is critical to achieving a compact encoding, because the average number of neighbors of a router in a real-world network is typically vastly smaller than the total number of routers in the network [3, 13]. By exploiting the structure of the real-world graphs, we are able to reduce the size of the encoding significantly compared with globally-unique labels.

For (b), we use the two fields: $\langle \text{code} \rangle$ and $\langle \text{length} \rangle$. Here, $\langle \text{length} \rangle$ specifies the total bit-lengths of all the labels d_1, \dots, d_ℓ of the alternate path. Based on our evaluation, alternate paths are shorter than 32 bits in most cases and always shorter than 128 bits; in cases a node has no alternate path, the alternate path bit-length is 0. Thus, for greater compactness, we make the bit-length of the $\langle \text{length} \rangle$ field be variable and store it in the $\langle \text{code} \rangle$ field using a prefix-free code, with the $\langle \text{code} \rangle$ bit sequences 0, 10, and 110 mapping to values of 5, 7, and 0, respectively.

The header contains two additional pieces of information. First, the SLICKPACKETS header begins with a two byte field, specifying its *header length*. Second, a one-bit field ON-ALTERNATE? specifies whether the packet is traversing along the primary path or an alternate path, and is initially false. We discuss next how routers use this information to forward packets.

3.4 Forwarding

We now describe the forwarding mechanism used by SLICKPACKETS routers for the Default format. The input to this mechanism is the SLICKPACKETS header described in §3.3, and the output is the interface out which the packet will be forwarded.

Upon receiving a packet, the router first checks the value of the SLICKPACKETS header length. If this is 0, this router is the destination for the packet. If not, the router checks the ON-ALTERNATE? bit to see whether it is on the primary path or on an alternate path. We describe the forwarding operations for the two cases separately.

Router on the primary path. The router reads the first segment in the header, which corresponds to itself, and inspects the primary next-hop label p . If the corresponding link available, the router deletes this first segment corresponding to itself. It also updates the header length by subtracting the length of its segment. The packet is then forwarded to the next-hop on the primary path with the new header.

If the primary next-hop link is not available, and the alternate path length is 0, the packet is dropped. Otherwise, the router reads its next-hop label d_1 on the alternate path. If the link corresponding to d_1 is not available, the packet is dropped.³ If the link is available, the router removes *all* segments in the header, replacing them by

²While the Default format could be generalized to have multiple alternates at a router, or segments within segments to provide alternates for routers along an alternate path, we do not explore that generalization here; in any case, such applications can use the Direct format.

³Or any other failure reaction mechanism can be applied.

its remaining alternate path labels (d_2, \dots, d_ℓ). It also updates the header length appropriately and sets the ON-ALTERNATE? bit. The packet is then forwarded to the next-hop via label d_1 .

Router on an alternate path. The router reads its next-hop label. If the corresponding link is not available, the packet is dropped (or, as earlier, some other failure reaction mechanism is employed). If the link is available, the router deletes its label from the header, updates the header length, and forwards the packet to the next-hop.

Simplifying forwarding operations. The above description involved removing a prefix of the header, and in the case of moving to an alternate path, a suffix as well. In some data plane implementations, these operations may be costly. In this case, we can simply add *start* and *end* pointers at the front of the header, indicating the extent of the remaining header. In an extra 3 bytes, we can fit two pointers that can point to individual bits in a 512-byte header (which is far larger than we need).

Interdomain vs. intradomain issues. In an intradomain deployment, we may assume that each router runs SLICKPACKETS and forwards packets as described above. However, in an interdomain deployment the forwarding subgraph roughly represents AS-level paths (as discussed in more detail in §3.1). When the packet is forwarded though an intermediate domain, that domain must forward the packet on to the next AS-level hop. Network operators may independently choose from a variety of ways to do this, for example by tunneling the packet with MPLS, or perhaps running SLICKPACKETS internally as well as interdomain.

4. EVALUATION

SLICKPACKETS advocates the idea of embedding a forwarding subgraph (FS) in the packet header, giving routers multiple forwarding options in order to provide the source with some property that it desires. While SLICKPACKETS can support flexible FS selections that provide different guarantees, for concreteness, this section evaluates the FS selection exemplified in §3.2, which targets fast reaction in the presence of single-link failures. The source constructs a DAG comprised of the shortest primary path, and the shortest alternate path for each node on the primary path in case that node’s outgoing link along the primary path fails. In terms of performance, three metrics are important: (a) encoding size, (b) failure reaction effectiveness, and (c) router complexity and packet forwarding rates. We present results for (a) and (b) in this section and discuss (c) in §7.

Topologies. We use three network topologies in our evaluation: the latency-annotated topology from Sprint ISP 1239 [2], with 315 nodes and 972 links; an AS-level map of the Internet [13], with 33,508 nodes and 75,001 links; and the largest component, with 190,914 nodes and 607,610 links, of a router-level map of the Internet [1]. The latter two topologies lack latency information; we take all links to have equal length. While using SLICKPACKETS directly on a router-level map of the Internet is not a likely deployment scenario (due to privacy and scaling issues, ASes do not propagate internal topologies globally in today’s Internet), we consider this extreme design point to investigate scaling issues of our design.

4.1 Encoding size

Since we encode the FS into the packet header, the **encoding size** determines the bandwidth overhead. We evaluate the resulting encoding sizes of the Direct and Default encoding formats presented in §3.3, for FSes constructed using the algorithm presented in §3.2.

Furthermore, regardless of the encoding format used, the **FS size**—the number of edges—is a factor influencing the encoding size. We are thus also interested in comparing the sizes of FSes constructed by the algorithm described in §3.2 to **lower bounds** on the sizes of FSes returned by any algorithm that provides shortest path latencies and single-link failure protection. These lower bounds impose a fundamental limit on the encoding size; intuitively, for a given encoding format that already uses optimized label lengths, it is hard to reduce the encoding size significantly without reducing the FS size. We describe in Appendix D an algorithm that yields a lower bound on the size of the FS for a given primary path hopcount.

Methodology. We evaluate all 98,910 possible ordered source-destination pairs of the Sprint topology. For the AS- and router-level topologies, we randomly sample ten million unique ordered source-destination pairs. For each pair, we record these values: the Default and Direct encoding sizes, the size of the FS constructed using our algorithm, and the lower bound on FS sizes.

Results. Fig. 4 shows the encoding size results. We see that Default has somewhat smaller size almost always; Direct performs noticeably better only in the extreme tail of the router-level topology. We therefore discuss Default in what follows. For the intradomain Sprint topology, the maximum encoding size is 58 bytes. The plot has a long tail with 90% and 99% of the source-destination pairs requiring less than 21 bytes and 34 bytes of encoding, respectively. For the interdomain AS-level map of the Internet, the maximum encoding size is 50 bytes. As with the Sprint topology, the plot has a long tail, with 90% of the source-destination pairs resulting in encodings of less than 21 bytes; 99% of the source-destination pairs result in less than 26 bytes.

For the extreme case of router-level topology, 90% of the source-destination pairs result in encodings of less than 43 bytes; 99% less than 60 bytes. The remaining less than 1% of the source-destination pairs constitute the long tail, with maximum encoding size of 132 bytes. Although the router-level realization of SLICKPACKETS may be impractical, the above results demonstrate that SLICKPACKETS can scale on graphs as large as 200,000 nodes with moderate increase in the packet header sizes. If desired, this overhead may be amortized over more data (e.g., by leveraging IPv6 jumbo frames) or using SLICKPACKETS only for application data that is most sensitive to failures.

Fig. 5 shows the FS size (in number of links) and lower bound. For the AS-level and router-level topologies, our FS size is very close to the lower bound; for the Sprint topology, the difference is somewhat larger. Overall, the results suggest that, for handling single-link failures, our simple FS selection algorithm is relatively close to optimal in terms of minimizing the number of links in the FS.

For the Sprint topology, there is also a long tail in both our FS sizes and the lower bounds. The reason is that

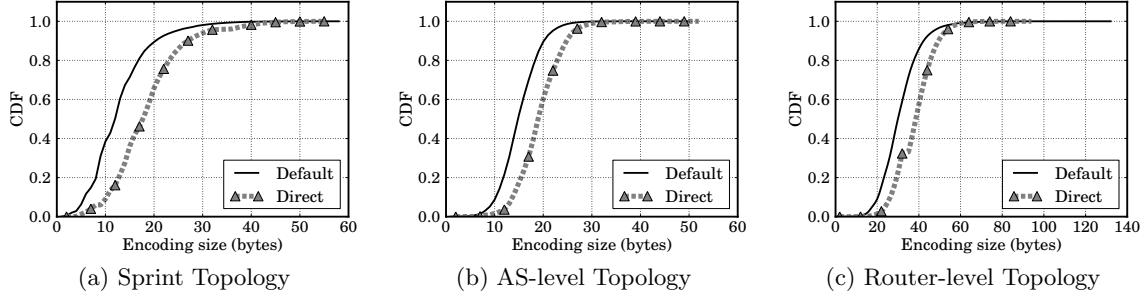


Figure 4: CDF of SLICKPACKETS encoding size in bytes for the Direct and Default encoding formats, for handling single-link failures.

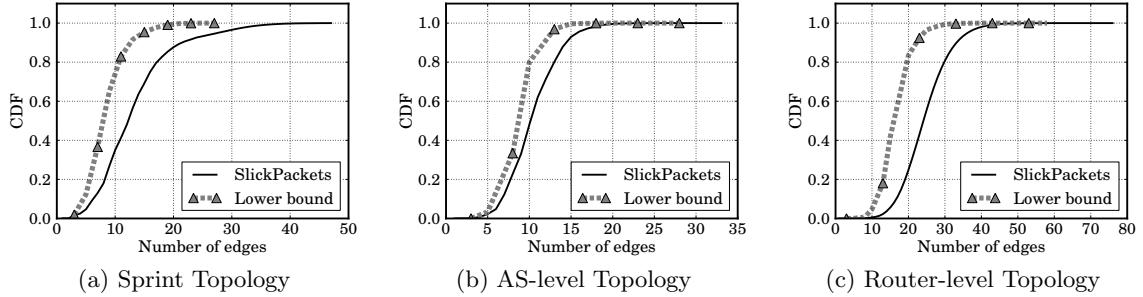


Figure 5: CDF of SLICKPACKETS FS size and the lower bound in number of edges for handling single-link failures.

there are a few source-destination pairs that have long primary paths, requiring alternate paths for a large number of nodes, resulting in larger number of edges.

4.2 Failure reaction effectiveness

One metric to evaluate the effectiveness of a failure reaction mechanism is the packet **stretch**, the ratio of the length of a packet’s path to the length of the shortest possible path. Previous works calculate stretch based on packets’ traversed path costs or transit times. However, for a delay-sensitive application, we are interested in the time a packet is *live* from the application’s perspective—from the time the packet is generated by the source application to the time it is received by the destination. Thus, we define the stretch for a packet that does not fully traverse the original shortest path, to be the ratio of the time the packet is *live* to the post-link-failure shortest path latency; for other packets—those that traverse the original shortest path—the stretch is 1. For brevity of the ensuing discussion, l_0 denotes the failed link on the primary path from source s to destination d ; r_0 denotes the router that is adjacent to and upstream from l_0 on the primary path; and t_0 denotes the time of failure of l_0 .

Modeling delay at network devices. A router in the network, upon a link failure, has to perform a number of tasks before it has new valid default next hops for affected destinations. The four major tasks are: (1) detecting a failed link (if the router is adjacent to the failed link) and generating a control plane message; (2) processing of received control packets; (3) computing the new shortest path tree (SPT); and (4) updating the forwarding information base (FIB). We assume that the delay in detecting

a failed link is zero since irrespective of the underlying routing architecture, all packets during this period are lost;⁴ this does not make a difference in our performance comparison results. We consider the three other major contributors.

Let d_r be the time spent by a router in processing a control packet (i.e., the time between the router’s receipt and forwarding of the packet). d_r (along with link latencies) dictates the propagation rate of control packets through the network. Let d_p be the delay between a router’s learning of the link failure and starting a new SPT computation; d_c be the time taken to compute the new SPT; and d_u be the time taken to update the FIB. Note that, upon receiving a control packet, a router necessarily spends $D = (d_p + d_c + d_u)$ time before having new valid default next hops for affected destinations. The values of d_c and d_u depend on the router architecture, algorithms in use, the topology, and the router’s location. Lacking a good model, we set these values to 0 in our simulations. However, we use $D = d_p = 50$ ms [18] and $d_r = 2$ ms [8, 9] for the Sprint topology. For the AS-level and router-level topologies, we use $D = d_r = 0$.

4.2.1 Failure reaction schemes

The performance of source routing protocols also depends on the *control plane* mechanism: the technique used to inform sources about the failures in the network. We describe three variants of SLICKPACKETS design with different control plane mechanisms. We also describe three

⁴Unless packets are duplicated along multiple paths—a design point that may be reasonable for certain kinds of traffic, but which we do not consider in this paper.

protocols—one from the SCR paradigm and two from the NCR paradigm—that we compare with SLICKPACKETS.

Flooded-SLICKPACKETS. Upon detecting the link failure, r_0 floods the network with a link state advertisement (LSA). This is similar to running an SCR protocol with an OSPF [21] style control plane mechanism.

Fast-SLICKPACKETS. When r_0 receives a packet whose primary next-hop traverses l_0 , it informs s about the link failure by directly sending an ICMP-style notification message to s . The rationale is that, to reduce control overhead, only sources that use l_0 in their primary paths need to be notified. Intuitively, this significantly reduces the control plane packets sent into the network.

e2e-SLICKPACKETS. The router r_0 piggybacks the link-failure information on the packet being forwarded on the alternate path towards d , which, upon receiving this information, may inform s of the link failure. Thus, failure information is sent to the source in an end-to-end manner.

All SLICKPACKETS schemes use the same FS selection algorithm (§3.2) and incur the delay D between learning of the failure and switching to new primary paths.

Vanilla source routing (VSR). For purposes of comparison with SLICKPACKETS, we evaluate a simple “vanilla” source routing protocol. In VSR, each source s specifies a single shortest path to its destination d in the packet header. For the control plane mechanism, we use the “fast” version, where r_0 directly notifies s . After receiving the notification, s incurs the delay D before computing a new shortest path. Without a valid path, packets generated during this time are queued. Packets that use l_0 in their paths will be dropped by r_0 after the link failure. However, once s has computed a new path, it resends the packets that would have been dropped, i.e., those that it sent in the time interval $[t - R, t]$ where t is the time s learned of the failure, and R is the RTT between s and r_0 . Note that for some of these resent packets, there could be two concurrent live copies: the resent copy that will be delivered along the new path, and the original copy that will be dropped when it reaches r_0 . This scheme may be difficult or undesirable to implement in practice, but as an idealized VSR, it is a useful comparison.

Ideal-SafeGuard. We simulated an idealized version of SafeGuard [18], a network-controlled routing protocol that achieves fast failure reaction. SafeGuard uses the standard OSPF as the control plane substrate. In SafeGuard, r_0 immediately uses pre-computed shortest alternate paths to quickly redirect packets that it would otherwise forward along l_0 . Other routers recognize redirected (“escort mode”) packets and forward them along their intended alternate paths; however, until they have updated their FIBs (after delay D after receiving the LSA), these routers continue to forward “normal mode” packets along their sub-optimal paths towards l_0 . In practice, the “alternative path databases,” which are found to be 2 to 8 times larger than a router’s intradomain FIB [18], might increase lookup latencies or be an impractical memory requirement. However, our ideal version of SafeGuard ignores these issues.

Ideal-NCR. This represents an ideal (and unachievable) NCR scheme, in which each router learns of a link failure in exactly the propagation delay along the shortest path from the point of failure to the router; and the router

instantly begins forwarding packets along the shortest alternate path. Ideal-NCR is equivalent to a special case of Ideal-SafeGuard where all delays, except propagation delay, are zero (i.e., $D = d_r = 0$).

4.2.2 Methodology

We wrote a static simulator for our evaluation purposes. The simulator uses the packet stretch computations described in Appendix A. Since we are evaluating the reaction to single-link failures, we evaluate only (l_0, s, d) triples where the primary path from s to d uses l_0 , and s and d remain connected after the failure of l_0 , so that at least one alternate path to d exists for each router upstream from l_0 . For the Sprint topology, we evaluate all 424,569 possible such triples. For each of the AS- and router-level topologies, we sample 1,000 random links and use a sampling algorithm (described in Appendix C) to obtain over 750,000 and 890,000 such triples, respectively.

In our simulations, the application at the source generates packets every 1 ms, starting at time $t = 0$ ms. For the time of link failure t_0 , however, recall that in Ideal-SafeGuard, Ideal-NCR, and Flooded-SLICKPACKETS, r_0 floods the LSA when it detects the link failure, not when it receives sources’ packets. For these schemes, the sooner the link fails, the sooner intermediate routers and the source learn of the failure and use better paths. So, for a fair comparison with non-flooding schemes, we consider two extreme points: when t_0 is greater than the network diameter in terms of *link latencies* and when $t_0 = 0$. The former case ensures that by the time t_0 , all sources in all evaluated (l_0, s, d) triples have had packets reaching r_0 . For the Sprint topology, with a diameter of 139 ms, we use $t_0 = 150$. For the AS- and router-level topologies, we assume all links have latencies 1 ms and use $t_0 = 50$.

4.2.3 Results

The high-level results reveal that SLICKPACKETS schemes (particularly the Fast and Flooded variants) achieve packet stretch comparable to that of NCR scheme Ideal-SafeGuard. Although SLICKPACKETS schemes take slightly longer to converge compared to SafeGuard, they avoid the high packet stretch of Fast-VSR.

Average stretch. Fig. 6 shows the packet stretch averaged over all evaluated (l_0, s, d) triples when t_0 is greater than the network diameter. We first consider features common to all schemes. For a given scheme, all packets generated early in the simulation have stretch 1. Gradually, as packets generated closer to t_0 , as well as more triples where s is closer to l_0 , are affected by the failure, the average stretch increases. Additionally, for any triple, all packets generated after t_0 have stretch no higher than those generated at t_0 ; this is reflected in the average stretch over all triples.

We now compare NCR and SLICKPACKETS schemes. In NCR schemes, routers upstream from l_0 , once they receive the LSA and update their FIBs, can redirect packets before they reach l_0 ; while in SLICKPACKETS schemes, packets have to reach l_0 before being redirected. This difference gives NCR schemes only a small advantage for early packets, especially for the Sprint topology in Fig. 6(a), because upstream routers still incur the delay D between receiving the LSA and updating their FIBs. For later packets, this advantage becomes more significant as more

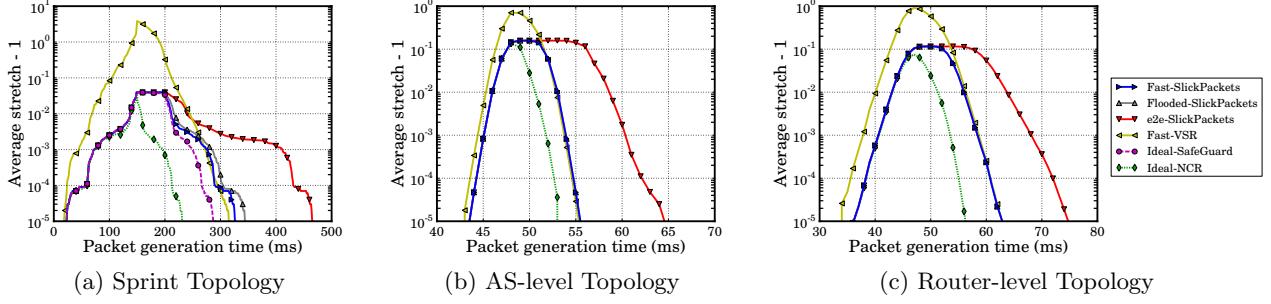


Figure 6: Average packet stretch - 1 vs. packet generation time when t_0 is greater than the network diameter. The y-axes are on log scales. For the Sprint topology, $t_0 = 150$, $D = 50$, $d_r = 2$. For the AS- and router-level topologies, $t_0 = 50$, $D = d_r = 0$.

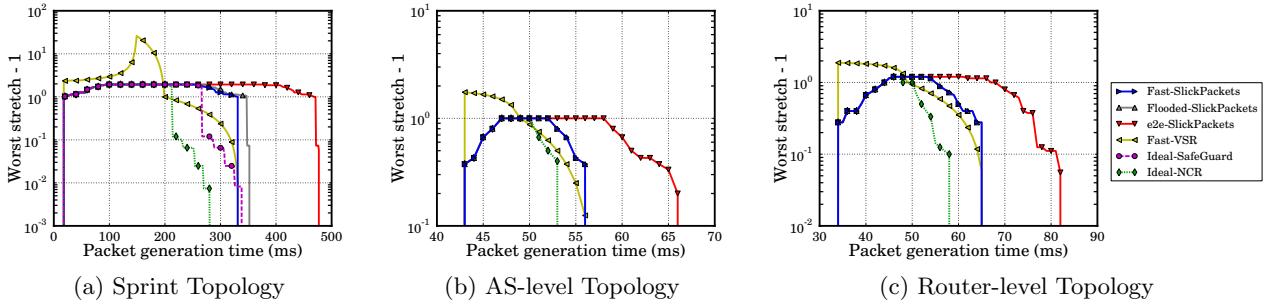


Figure 7: Worst packet stretch vs. packet generation time when t_0 is greater than the network diameter. The y-axes are on log scales. For the Sprint topology, $t_0 = 150$, $D = 50$, $d_r = 2$. For the AS- and router-level topologies, $t_0 = 50$, $D = d_r = 0$.

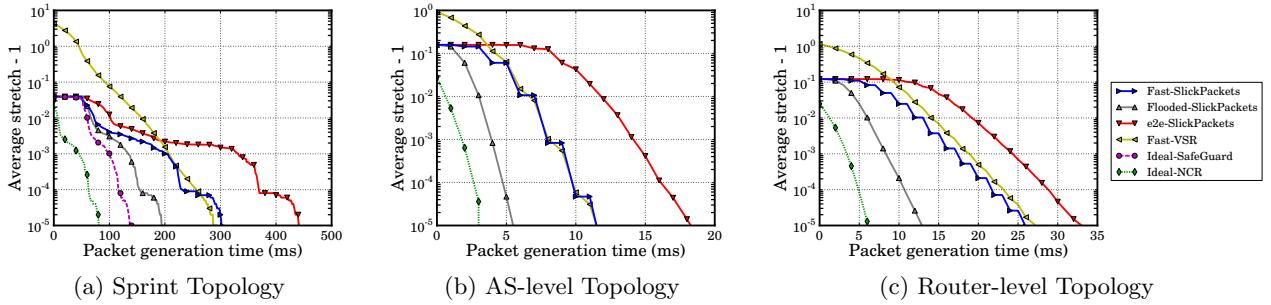


Figure 8: Average packet stretch - 1 vs. packet generation time when $t_0 = 0$. The y-axes are on log scales. For the Sprint topology, $D = 50$, $d_r = 2$. For the AS- and router-level topologies, $D = d_r = 0$.

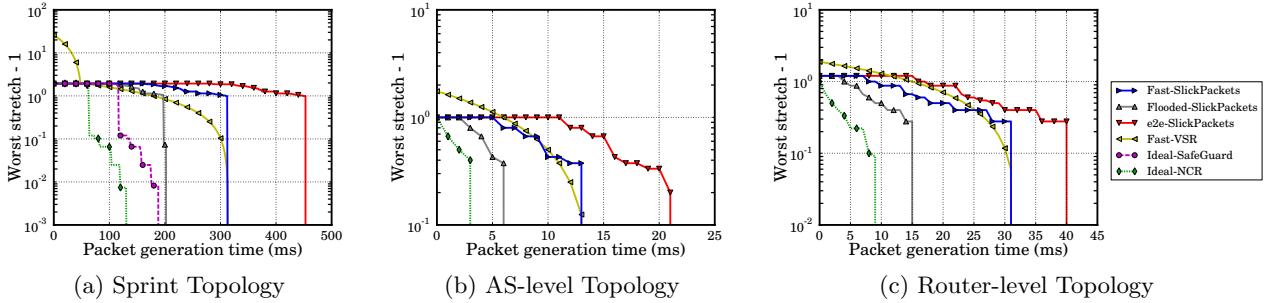


Figure 9: Worst packet stretch vs. packet generation time when $t_0 = 0$. The y-axes are on log scales. For the Sprint topology, $D = 50$, $d_r = 2$. For the AS- and router-level topologies, $D = d_r = 0$.

upstream routers update their FIBs. As expected, Ideal-NCR is the best performing scheme in all three topologies: it converges 57 ms before Ideal-SafeGuard for the Sprint topology (due to $D = 50$ and $d_r = 2$) and is equivalent to Ideal-SafeGuard (not shown) in the other two topologies, where $D = d_r = 0$.

Consider the SLICKPACKETS schemes in Fig. 6(a). We see that for packets generated between $t_0 = 150$ and $t_0 + D = 200$, the average packet stretch is (1) constant within the same scheme and (2) identical across all schemes. Recall that all SLICKPACKETS schemes use the same FS selection algorithm and incur the same delay D between learning of the failure and switching to new primary paths. Thus, the only factor affecting their relative performances is the time s learns of the failure, which is determined by the relative distances among l_0 , s , and d for different triples in the same scheme, and the different control schemes given the same triple. So, regardless of the (l_0, s, d) triple or the control scheme, there is a minimum window of D time where s uses the same (old) primary path. After this window, we can see that Fast-SLICKPACKETS converges slightly faster than Flooded-SLICKPACKETS because the LSAs in Flooded-SLICKPACKETS incur delay d_r at intermediate routers; in Fig. 6(b) and (c), where $d_r = 0$, Fast- and Flooded-SLICKPACKETS are identical. And both of them converge significantly faster than e2e-SLICKPACKETS as expected.

Finally, we see that in Fast-VSR, early packets experience higher stretch than in other schemes. This is because these packets are dropped and have to be resent by s . They experience on average a delay of one half the RTT between s and r_0 , plus the delay D before being sent along the new path, resulting in a high stretch. However, Fast-VSR can catch up to and overtake Fast-SLICKPACKETS for two reasons. First, consider the packet sent 1 ms before s learns of the failure: in Fast-VSR, it is delayed $(1 + D)$ ms before being resent along the new path; while in Fast-SLICKPACKETS, the amount of time this packet traverses the original primary path only to be redirected backwards can be larger than $(1 + D)$, especially if both the primary path and alternate path contain a very high latency link. Second, consider the packet generated 1 ms before s has a new primary path: in Fast-VSR, it is delayed (queued) only 1 ms before being sent on the new optimal path; while in Fast-SLICKPACKETS, this packet will be sent along the original primary path and will be redirected, experiencing a higher stretch than its Fast-VSR counterpart. These two effects enable Fast-VSR to noticeably overtake Fast-SLICKPACKETS in Fig. 6(a), but in Fig. 6(b) and (c), where $D = 0$ and all links have latencies 1 ms, these two effects are less pronounced.

Worst stretch. Fig. 7 shows the worst stretch of packets given their generation time, among all evaluated (l_0, s, d) triples, when t_0 is greater than the network diameter. Note that the simulation-wide worst stretches for all schemes except Fast-VSR are equal, which are 2.93, 2.0, and 2.2 in Fig. 7(a), (b), and (c), respectively. This is because all these schemes do not drop packets, so the worst stretch is that of packets that r_0 redirects, which is the same for all these schemes. Also note that for schemes that do not drop or queue packets, the worst stretch occurs when a packet traverses the maximum possible distance along the original shortest path without reaching d , is redirected

back to s , and traverses the shortest alternate path. So, 3 is the upper-bound stretch because the shortest alternate path cannot be shorter than the original shortest path.

For the Sprint topology in Fig. 7(a), the simulation-wide worst stretch for Fast-VSR is 27. This happens to packets sent right before $t_0 = 150$ in triples where s is close to d , so that the time duration D that these packets are delayed dominates the latencies of the original and post-link-failure shortest paths. In the AS- and router-level topologies, where $D = 0$, the simulation-wide worst stretch of Fast-VSR are 2.75 and 2.88 respectively.

When $t_0 = 0$. Fig. 8 and 9 show the results for when $t_0 = 0$. The overall behavior of each individual scheme exhibits similar patterns to when t_0 is greater than the network diameter. The differences are that the peak stretches occur for packets generated at $t_0 = 0$. Furthermore, as expected, flooding schemes benefit from the earlier time of failure: for example, for the Sprint topology in Fig. 8(a), Ideal-NCR and Ideal-SafeGuard converge further ahead of Fast-SLICKPACKETS compared to Fig. 6(a), and even Flooded-SLICKPACKETS now converges ahead of Fast-SLICKPACKETS (similarly for the AS- and router-level topologies).

In terms of simulation-wide worst stretch, those of non-flooding schemes (Fast- and e2e-SLICKPACKETS as well as Fast-VSR) are the same as when t_0 is greater than the network diameter. This is as expected because for these schemes, it is still r_0 that redirects packets and/or triggers the notification of sources. For flooding schemes, however, it can be expected that simulation-wide worst stretch would be lower compared to when t_0 is greater than the network diameter. Nevertheless, the Sprint topology contains triples where an upstream link that is close to r_0 has very high latency compared to the distance between s and r_0 , so that s 's first packet does not benefit from the flooded LSA: it still has to reach r_0 before being redirected. This results in the simulation-wide worst stretch of 2.93 in Fig. 8(a).

5. DISCUSSION: FORWARDING SUBGRAPH SELECTION

The SLICKPACKETS design is agnostic to how the source selects the forwarding subgraph (FS). For example, the FS selection may be guided by demands of the application running at the source (for example, if the source is an end host) or the performance goals of a network operator (for example, if the source is an edge router). In this paper, we presented and evaluated one such FS selection algorithm: where the FS allows re-routing of packets within the network in case of single-link failures. We now discuss alternative FS selection strategies.

Handling node failures. For the FS to handle node failures, we need only a simple modification to the link-failure-avoiding FS selection of §3.2. A source s , for a given destination d , constructs the FS in three steps. First, s computes a primary path P to d by running an instance of the shortest path algorithm. Next, to protect against single *node* failures, s visits each node along P , and computes the alternate path P_i it would prefer the packet to be routed along if that node were to fail. In particular, for each node v_i on the primary path with node v_{i+1} as the next hop along the primary path, we (a) re-

move v_{i+1} ; (b) compute a shortest path from v_i to d ; and, (c) restore v_{i+1} .

Handling multiple link failures. A source may desire to construct an FS that protects against multiple link failures. This may be done by extending the scheme from §3 to construct an FS that protects from multiple edge-failures. For example, it may be sufficient to have two strategically chosen alternate paths for all nodes on the primary path. The idea is that the source can choose alternate paths that are not failure-correlated with the primary path. This may allow a much larger amount of resiliency; although the performance evaluation of such a scheme is subject to future work.

Congestion avoidance. Our focus in this work so far has been on dealing with failures. However, alternate paths in the FS may also be used to react to congestion in the network. For example, intermediate routers along the path may choose to forward the packet along an alternate path if the primary path is congested (e.g., if the interface queue for the corresponding link is filled beyond a particular threshold). Using a FS also enables the source to optionally provide control over load balancing, by providing feedback on which set of paths are tolerable for the load balancing process.

6. RELATED WORK

Our goals are related to two key areas of related work:

Failure reaction in network-controlled routing protocols. There has been much work on coping with failures in IP networks. We focus on the most closely related work: protocols that guarantee packet delivery in the presence of one or more link failures. R-BGP [16] constructs interdomain backup paths to handle single link failures, given some assumptions about routing policies. SafeGuard [18] uses a remaining path cost field in a packet as a heuristic to determine whether the path expected by the previous hop is different than the path available to the current hop. In this way, it can decide when to reroute packets along pre-computed backup paths. FCP [17] takes a different approach to determining when packets should be rerouted: each packet carries a list of the failed links it has encountered. The best backup paths are computed on the fly at routers, thus allowing FCP to be robust to multiple link failures, but requiring fairly heavyweight graph processing in the data plane. MPLS Fast Reroute [22] relies on precomputation of backup paths. In its local repair variant, an additional path is constructed to avoid each neighboring link or node, which can inflate storage requirements and will not result in lowest-stretch backup paths. As discussed in the introduction, all of the above approaches are NCR protocols, which do not permit source control of primary or backup paths. In addition, backup paths are computed or stored at every router within the network, so that there is a dependency between each router’s forwarding table and the topology of the entire network.

One way to get a small amount of route control at the source within an NCR architecture is to use multihoming: the source can then select between several providers [4]. This could be used to enable some source control, while still applying the NCR resilience techniques described above. However, this provides only a very limited amount of con-

trol to the source, and does not yield the full benefits of source control described in the introduction. Moreover, if many sources are multihomed, this vastly increases routing state within the network, since each router would be required to know about every point of multihoming attachment if we desire to provide alternate paths that avoid a failure of one of these links.

Our use of routing along FSes was inspired by [19], which argues that a directed acyclic graph is a better forwarding architecture than the more traditional shortest-path tree. While [19] focuses on improving NCR schemes, we target achieving the benefits of both network- and source-controlled routing. Additionally, while [19] will deliver every packet even during link failures, it does not guarantee the latency that these packets will have. SLICKPACKETS can guarantee that for single-link failures, packets will follow the shortest alternate path from the point of failure to the destination.

Source routing. There is also a large body of work on source controlled routing, ranging from dynamic source routing in wireless networks [15] to future interdomain routing architectures [10, 20, 29, 30]. Two of these, Routing Deflections [30] and Path Splicing [20], target fast re-routing within the network. Both use path label bits set by the source to pseudorandomly select a next hop at each router or AS. In [20], pseudorandom forwarding can lead to forwarding loops. In [30] routers follow certain rules that ensure loop-freedom, but reduce path diversity.

There are three important differences between [20, 30] and SLICKPACKETS. First, [20, 30] do not fully support source control over primary or backup routes; although sources can select among some set of paths, they cannot tell which paths they are selecting. Second, although packets can be rerouted quickly within the network after a link failure, this is not guaranteed (packets may be dropped), and the backup paths are not guaranteed to have optimal latency. Third, [20, 30] are similar to traditional NCR schemes in terms of the state in the network; indeed, [20] increases forwarding table size because each router stores multiple next-hops for each destination. In contrast, SLICKPACKETS enables source control, can guarantee resilience⁵ to single-link failures with packets sent along the shortest alternate path from the point of failure to the destination, and requires only local state at routers.

Giving sources control over constructing end-to-end paths introduces a number of practical questions, for example in terms of policy compliance, security, and scalability of disseminating topological state. For these questions, we rely on previous work (e.g., [10, 29], and citations within), which provide solutions to these problems.

7. CONCLUSION

In this paper, we presented SLICKPACKETS, an approach to routing that attains failure reaction, while simultaneously retaining the benefits of source routing. SLICKPACKETS works by compactly encoding a set of alternate paths into data packet headers as a *directed acyclic graph*. Towards this goal, we provide simple algorithms for computing efficient graphs, and for encoding them into packets in a manner that can be processed by intermediate routers in an efficient manner.

⁵Unless, of course, no alternate path exists.

One major area left for future work is to evaluate the complexity of implementing SLICKPACKETS in production routers, and achievable packet forwarding rates; a key challenge here is dealing with increased header size. A promising avenue for evaluation is the Supercharged PlanetLab Platform [25], a network processor-based platform on which John DeHart has implemented a prototype version of SLICKPACKETS.

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APPENDIX

A. COMPUTING PACKET STRETCH

We describe here the stretch computations our simulator in §4.2.2 uses. Given a source-destination pair s, d and a failed link l_0 on the primary path between s and d , we wish to compute the stretch experienced by each packet that the application at source s generates. We assume the application at s generates packets every 1ms, starting at time $t = 0$. Further, we assume that all nodes in the network have sufficient queue space so that no packet is dropped for lack of queue space, and that the nodes can fully flush their queues/buffers instantaneously. We assume links have sufficient capacity and devices have sufficient data-plane processing capabilities, so that they do not introduce delays to data packets.

First, we give an overview of our approach (notation summarized in Table 1). For a given (l_0, s, d) triple in Fig. 10, consider a router r on the primary path that is upstream from l_0 . After the failure of l_0 , router r can “offer” two types of stretch to packets that reach it: (a) to packets that r redirects along its alternate path to d , a fixed stretch $\sigma(r)$; (b) to packets that r forwards along its primary path, whatever stretch offered by downstream routers on the primary path. The two important features of a router r are then the time $\tau(r)$ at which it starts redirecting packets along its alternate path, and

Notation	Description
l_0	a failed link on the primary path from source s to destination d
r_0	the node upstream from and adjacent to l_0 (r_0 might be source s itself)
t_0	the time of failure of link l_0
$t_{learn}(u)$	the time a node u learns of the failure, by detecting it or being notified ($t_{learn}(u) \geq t_0$)
$\tau(u)$	the time a node u can start sending packets along the post-failure shortest path from u to d
$\sigma(u)$	the stretch experienced by packets that a node u sends along the post-failure shortest path from u to d
$dist(u, v)$	the shortest path latency between nodes u and v with no link failure
$\widehat{dist}(u, v, l)$	the shortest path latency between nodes u and v after the failure of link l
$h(u, v)$	the hop-count between nodes u and v with no link failure

Table 1: Notation used in the packet stretch computations

the fixed stretch $\sigma(r)$ it offers such redirected packets. Then, given $\tau(r)$, we can compute the sent time of the first packet from s that will be redirected by r ; packets sent before this packet will be forwarded to r 's primary next-hop and thus experience whatever stretch offered by r 's downstream routers. Applying the above analysis to all routers upstream from l_0 , our simulator determines the stretch experienced by any packet given the time it is generated by the source application.

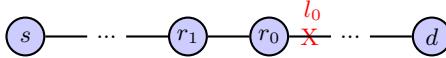


Figure 10: A primary path from s to d with failed link l_0 . r_0 is the router upstream from and adjacent to l_0 .

A.1 SLICKPACKETS

With all SLICKPACKETS variants, for a particular (l_0, s, d) triple, the only two nodes that potentially redirect packets are r_0 and source s , so we only need to analyse these two nodes.

Consider r_0 . It starts redirecting packets at time $\tau(r_0) = t_0$. The first packet from s that will be redirected by r_0 arrives at r_0 at time $\max\{t_0, dist(s, r_0)\}$ and thus is sent/generated by s at time

$$\max\{t_0, dist(s, r_0)\} - dist(s, r_0) \quad (1)$$

This packet and all packets redirected by r_0 experience its fixed stretch, which is

$$\sigma(r_0) = \frac{dist(s, r_0) + \widehat{dist}(r_0, d, l_0)}{\widehat{dist}(s, d, l_0)} \quad (2)$$

Consider s . It is easy to see that

$$\sigma(s) = 1 \quad (3)$$

To compute the time that s first “redirects” packets—sends them along its new primary path to d —note that for all SLICKPACKETS variants, this time is

$$\tau(s) = t_{learn}(s) + D$$

Now, we show the derivation of $t_{learn}(s)$ for each SLICKPACKETS variant.

Flooded-SLICKPACKETS. At time t_0 , when it detects the link failure—not when it receives packets from source

s —the router r_0 floods the network with the LSA. Thus, s receives the LSA and learns of the link failure at time

$$t_{learn}(s) = t_0 + dist(r_0, s) + h(r_0, s) \cdot d_r \quad (4)$$

Fast-SLICKPACKETS. Upon receiving a packet from s that requires redirection, r_0 sends a notification message to s about the failed link. Thus, s receives the notification message and learns of the link failure at time

$$t_{learn}(s) = \max\{t_0, dist(s, r_0)\} + dist(s, r_0) \quad (5)$$

e2e-SLICKPACKETS. Upon receiving a packet from s that requires redirection, r_0 piggybacks the notification message in the packet on the way to d , which receives the packet at time $\max\{t_0, dist(s, r_0)\} + \widehat{dist}(r_0, d, l_0)$. After d computes its new shortest path to s , it sends the notification message to s . Thus, s receives the notification message and learns of the link failure at time

$$t_{learn}(s) = \max\{t_0, dist(s, r_0)\} + \widehat{dist}(r_0, d, l_0) + D + \widehat{dist}(d, s, l_0) \quad (6)$$

A.2 Ideal-SafeGuard

At time t_0 , when it detects the link failure—not when it receives packets from s —the router r_0 floods the network with the LSA. As routers upstream from r_0 learn about the link failure, they can potentially redirect packets along shorter paths, reducing the amount of time packets traverse a sub-optimal path, i.e., packets do not have to reach the failure before being redirected.

Consider r_0 . It learns of the link failure at time t_0 . Because it has already pre-computed alternate paths to d , it can immediately redirect packets along the alternate path. Thus the first packet from s that will be redirected by r_0 arrives at r_0 at time $\max\{t_0, dist(s, r_0)\}$ and thus is sent/generated by s at time

$$\max\{t_0, dist(s, r_0)\} - dist(s, r_0) \quad (7)$$

This packet and all packets redirected by r_0 experience its fixed stretch

$$\sigma(r_0) = \frac{dist(s, r_0) + \widehat{dist}(r_0, d, l_0)}{\widehat{dist}(s, d, l_0)} \quad (8)$$

Consider a node r upstream from r_0 . (r can be a router or source s .) It learns of the link failure at time

$$t_{learn}(r) = t_0 + dist(r_0, r) + h(r_0, r) \cdot d_r$$

Because it is not adjacent to the failed link, r only starts redirecting packets along its alternate path to d at time $t_{learn}(r) + D$. Thus, the first packet from s that will be redirected by r along the alternate path is sent by s at time

$$\max\{0, t_{learn}(r) + D - \text{dist}(s, r)\} \quad (9)$$

This packet and all packets redirected by r experience its fixed stretch

$$\sigma(r) = \frac{\text{dist}(s, r) + \widehat{\text{dist}}(r, d, l_0)}{\text{dist}(s, d, l_0)} \quad (10)$$

Next, consider two adjacent routers r and r' upstream from l_0 where $r' \neq r_0$ and r is upstream from r' . Let t and t' , given by Eq. 9, be the sent times of the first packets from s that are redirected by r and r' , respectively. Note that $\text{dist}(r_0, r) > \text{dist}(r_0, r')$, $h(r_0, r) > h(r_0, r')$, and $\text{dist}(s, r) < \text{dist}(s, r')$; thus $t \geq t'$ ($t = t' \Leftrightarrow t = t' = 0$). If $t > t'$, packets sent by s in the interval $[t', t]$ are redirected by r' and thus experience the stretch offered by r' .

A.3 Fast-VSR

Unlike SLICKPACKETS and SafeGuard, with VSR, the router r_0 drops instead of redirecting packets; source s has to resend those dropped packets. Also, the only node that “redirects” packets is source s —it sends them along a new primary path. Furthermore, s queues packets generated by the application between the times it learns of the failure and is ready to use a new path to d . Thus, we only consider source s , but we consider two types of packets: those that are dropped and resent, and those that are queued.

The first packet from s that will arrive at r_0 after the link failure—thus will be dropped by r_0 and later resent by s —arrives at time $\max\{t_0, \text{dist}(s, r_0)\}$ (and thus is originally sent by s at time $\max\{t_0, \text{dist}(s, r_0)\} - \text{dist}(s, r_0)$). Upon receiving this packet, r_0 sends a notification message to s , which s receives at time

$$t_{learn}(s) = \max\{t_0, \text{dist}(s, r_0)\} + \text{dist}(s, r_0)$$

Thus, s is ready to use a new primary path to d at time

$$\tau(s) = \max\{t_0, \text{dist}(s, r_0)\} + \text{dist}(s, r_0) + D$$

At this time, s instantaneously resends all packets that would have been dropped. These packets were originally sent at time

$$\max\{t_0, \text{dist}(s, r_0)\} - \text{dist}(s, r_0) + \Delta \quad (11)$$

with $\Delta \in [0, 2 \cdot \text{dist}(s, r_0))$ (recall “[$t - R, t]$ ” in §4.2.1) and thus experience stretch

$$\frac{2 \cdot \text{dist}(s, r_0) - \Delta + D + \widehat{\text{dist}}(s, d, l_0)}{\widehat{\text{dist}}(s, d, l_0)} \quad (12)$$

For the queued packets, after learning of the failure, s queues all packets newly generated by the source application until it is ready to use a new primary path. These packets are generated between $t_{learn}(s)$ and $\tau(s)$. In other words, they are generated at time

$$t_{learn}(s) + \Delta \quad (13)$$

with $\Delta \in [0, D]$. Since s also instantaneously sends all these queued packets at $\tau(s)$, these packets experience

stretch

$$\frac{D - \Delta + \widehat{\text{dist}}(s, d, l_0)}{\widehat{\text{dist}}(s, d, l_0)} \quad (14)$$

Note that the packet generated at time $t_{learn}(s) + D$ has stretch 1, as is expected.

B. DIRECT ENCODING

Direct Encoding embeds the Forwarding Subgraph (FS) as a directed acyclic graph data structure in the packet header. At a high level, each router in the FS—except the destination router because it has no outgoing links—is encoded exactly once in a structure we call the **NodeDescriptor** (ND), at some location (bit offset) within the encoding. A router’s **NodeDescriptor** (ND) contains **SuccessorDescriptor** (SD) structures, which represent the router’s next-hop successor(s). A **SuccessorDescriptor** (SD) contains (1) the router’s *locally unique link identifier* for the next-hop successor and (2) the offset pointer to the successor’s ND. Finally, the packet header contains a “current node offset pointer”. A router reads this pointer to locate its ND, and updates it to point to the next hop’s offset pointer before forwarding.

We use the overall format:

NodePtrLength	CurrentNodePtr	ND_1	ND_2	\cdots	ND_k
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NodePtrLength A prefix code that indicates the length in bits of the **CurrentNodePtr** field and all other absolute node pointers. The mappings are 0, 10, 110, and 1110, for 10, 8, 6, and 4 bits respectively.

CurrentNodePtr This value specifies the bit offset (from the beginning of the encoding) of the current router’s ND. The value of zero has a special meaning: the current router is the final destination/egress router.

An ND can have either one or two SD’s, with the convention that the first successor is the primary one. The ND has the following format:

NumberOfSuccessors	SD_1	SD_2
--------------------	--------	--------

NumberOfSuccessors (1 bit) 0 indicates there is one successor, and 1 indicates there are two successors.

The SD contains two main pieces of information: the next-hop identifier and the offset pointer to its ND. For the next-hop identifier, similar to the encoding scheme discussed in §3.3, we use the router’s *locally unique link identifiers*, which it advertises as part of the network map dissemination. For the offset to the next-hop’s ND, we use a 1-bit flag to indicate that the next-hop’s ND immediately follows the current ND; otherwise, we include an absolute offset pointer to the next-hop’s ND. Here is the SD format:

LinkId	ContainsPtr?	Ptr
--------	--------------	-----

LinkId The identifier of the link to forward the packet. The length of this field is specified by the router as part of the map dissemination. In our encoding size evaluation (§4.1), we assume that it is $\lceil \log_2 \Delta \rceil$ bits.

ContainsPtr? (1 bit) 0 indicates that the next-hop’s ND follows immediately after the current router’s ND.

Ptr Pointer to the next-hop’s ND. The Length of this field is specified by **NodePtrLength** discussed above.

The 1-bit flag is only an optimization that allows us to leave off the offset to the next-hop’s ND. To make this optimization useful, the encoding algorithm first encodes all nodes on the primary path one after another. The first (primary) SD of each of these uses the 1-bit flag because the successor’s ND immediately follows its own descriptor (except in the penultimate router’s case, which uses an absolute pointer value of zero). The second SD, if any, uses the absolute offset pointer.

After encoding all nodes on the primary path, the encoding algorithm picks one of the alternate paths and encodes all of its yet-to-be-encoded nodes one after another. These nodes that are encoded contiguously can use the relative pointer for their SD’s, and when a node’s next-hop successor is an already-encoded node, then the next-hop successor’s offset pointer is used. Also, the penultimate router uses an absolute pointer value of zero in its SD.

Forwarding Algorithm. Upon receiving a packet, the router first gets the value of the **CurrentNodePtr** (after parsing **NodePtrLength**). If the value is zero, then the router is the egress router, and it can perform appropriate actions on the packet (e.g., delivering it on attached networks), and it does not forward the packet further.

If **CurrentNodePtr** has a non-zero offset value, then the router parses its ND at that offset. Note, the router expects that the lengths of its **LinkId** fields are what it advertised (e.g., $\lceil \log_2 \Delta \rceil$ bits). With that information, the router can fully parse its ND. If the link labeled in the first SD is online, then the router will use that link to forward the packet. Otherwise, if there is a second SD and its link is online, then the router will use that link to forward the packet. Otherwise, the router drops the packet.

Before forwarding the packet, the router needs to update the **CurrentNodePtr**. If the used SD contains an absolute offset pointer (i.e., its **ContainsPtr?** flag is 1), then the router updates **CurrentNodePtr** with the value in the SD’s **Ptr**:

$$\text{CurrentNodePtr} \leftarrow SD.Ptr$$

Otherwise, the successor’s ND follows immediately after the current router’s ND, so to obtain the successor’s ND offset, the router adds the total length of its own ND to its own (**CurrentNodePtr**) offset, and then updates **CurrentNodePtr** with that value:

$$\text{CurrentNodePtr} \leftarrow |ND| + \text{CurrentNodePtr}$$

C. SAMPLING ALGORITHM FOR SIMULATION

For each sampled link l_0 , we evaluate “qualified sources”: those whose shortest path tree (SPT) includes l_0 . To find

qualified sources, we sample up to 2,000 random sources and use the first 100 qualified sources, or fewer if we find fewer qualified sources. For each qualified source s , we randomly sample 100 destinations from among all those on the subtree of s ’s SPT that uses l_0 . Finally, among the sampled destinations, we use only those that remain connected with s after removing l_0 .

D. LOWER BOUND ON EDGE-SET SIZE

How much can we reduce the size of the FS by designing more sophisticated algorithms for selecting the FS? How close are the results given in §4 to the smallest possible header for handling single link failures?

In order to be able to answer the above questions, we derived lower bounds on the edge-set size of FSs that provide fast failure reaction against single link failures. That is, for any FS that uses the shortest path between the source and the destination as the primary path, the lower bound gives the minimum number of edges that the FS must contain in order to provide an alternate path avoiding any single-link failure on the primary path. For any source-destination pair s, d , the lower bound is given as follows:

$$\begin{cases} 2|P(s, d)| + 1 & \text{if graph weighted} \\ \left\lceil \frac{5|P(s, d)|}{2} \right\rceil & \text{if graph unweighted} \end{cases}$$

where $P(s, d)$ is the primary path and $|P(s, d)|$ the number of edges in $P(s, d)$. These lower bounds impose a fundamental limitation on the header size of SLICKPACKETS; intuitively, it is hard to reduce the header size (in bytes) significantly without reducing the edge-set size of the resulting FS. We prove the lower bound below.

Note that a trivial lower bound on the size of the FS is $2|P(s, d)|$ because each node in the primary must have two outgoing edges in order to provide fast failure reaction against single link failures. Theorem 1 essentially states this bound along with an example graph demonstrating that the bound is tight. However, if the graph is unweighted (all edges have the same weight), we can provide a better bound: intuitively, the alternate paths must include extra edges in order to ensure that they are at least as long as the primary (which is by definition the shortest). We give this improved bound in Theorem 2. We assume, in the following proofs, that the graph is not a multigraph and is 2-connected.

THEOREM 1. Suppose the FS uses the shortest path $P(s, d)$ as the primary path and can avoid any single link failure along the primary path. Then the FS has at least $2|P(s, d)| + 1$ edges. Moreover, there exist graphs for which this bound is tight.

PROOF. For weighted graphs, we note that FS contains $|P(s, d)|$ edges along the shortest path. Furthermore, each node along the shortest path requires at least one additional outgoing/incoming edge in order to provide fast reaction against single link failures. The proof follows by noting that there are exactly $|P(s, d)| + 1$ nodes along the shortest path. To prove tightness of the bound, we use the graph shown in Fig. 11. \square

Before going to the lower bound proof for unweighted graphs, we give some definitions to make the discussion

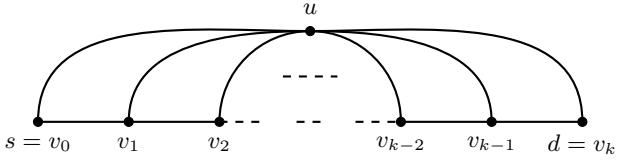


Figure 11: A graph that achieves the lower bound on the size of the FS for weighted graphs. The weight of edges (v_i, v_{i+1}) are all 1; the weight of edges (v_i, u) is set to $k - i$.

more succinct. Let $G = (V, E)$ be the graph and given a pair of vertices s, d , let FS be the optimal FS, meaning it has the minimum possible number of edges while satisfying the conditions in the theorem. Denote the shortest path between s and d as

$$P = P(s, d) = (s = v_0, v_1, \dots, v_{k-2}, v_{k-1}, v_k = d)$$

and let $|P|$ be the number of edges in P . Let $G' = (V, E')$ be a densest graph (with maximum possible number of edges) such that P is also the shortest between s and d in G' and let FS' be the optimal forwarding subgraph between s and d in G' . Let $|FS|$ and $|FS'|$ be the edge-set size of the optimal forwarding subgraphs FS and FS' . Let $Q(u, v)$ denote the shortest alternate path (as computed in §3) between any pair of nodes u and v and $N(u)$ be the set of neighbors of any node u .

THEOREM 2. *Under the same conditions as Theorem 1 except that edges have equal weights, the number of edges in the FS is lower bounded by:*

$$\left\lceil \frac{5|P(s, d)|}{2} \right\rceil$$

Moreover, there exist graphs for which the bound is tight.

PROOF. We start with a few simple observations: first, since $E \subseteq E'$, we have that $|FS| \geq |FS'|$. Hence, a lower bound on $|FS'|$ implies a lower bound on $|FS|$. Second, since G' is unweighted, there is no edge between v_i and v_k for any $i < k - 1$ otherwise P cannot be the shortest path. Furthermore, to provide fast failure reaction against single link failures, FS' must contain an edge (u, v_k) for some $u \notin P$ since $(v_{k-1}, v_k) \in P$ and the graph is not a multigraph.

Consider nodes u and v_{k-1} . Since the graph is not a multigraph, we have that $|Q(v_{k-1}, v_k)| \geq 2$. Hence, we can replace $Q(v_{k-1}, v_k)$ by (v_{k-1}, u, v_k) without increasing $|FS'|$; the edge (u, v_k) indeed exists as argued earlier. Now, consider node v_{k-2} . Note that $|Q(v_{k-2}, v_k)| \geq 2$ and hence, we can replace $Q(v_{k-2}, v_k)$ by (v_{k-2}, u, v_k) as earlier.

We make a final observation: let us denote by $FS' \setminus P$ the set of nodes that are in the FS' but not in P . We claim that for any node $q \in FS' \setminus P$, $N(q) \cap P \leq 3$. To prove this, suppose by way of contradiction that $N(q) \cap P \geq 4$. Then at least two of the nodes in $N(q)$ are at distance at least 3 along P , while they are connected via q by just two hops, contradicting the fact that P is the shortest path.

To summarize, we have shown that for any node $q \in FS' \setminus P$, we have that $N(q) \cap P \leq 3$. We have also proved

that in the (new) optimal FS, v_{k-2} and v_{k-1} are connected to a node u that has a direct link to d . Note that $u \in FS' \setminus P$ and it is already connected to three nodes in P . Hence, in the (new) optimal FS, we have that every node $v_i \in P$, $i < k - 2$ must find an alternate path to at least one of the nodes v_{k-2}, v_{k-1}, v_k or q and cannot have a direct (alternate) edge to any of these nodes. We create a new graph G'' by collapsing the four vertices $(v_{k-2}, v_{k-1}, v_k, q)$ (call this new node d'); to compute an optimal FS on G' , we can compute an optimal FS on G'' and combine it with the edges between these nodes that form a part of FS' . Hence, we have reduced our problem to a strictly smaller subproblem with the same constraints. This allows us to use a simple recursion. Let $S(n)$ denote the edge-set size of the optimal FS in G' with $|P| = n$. Then, we get the following recursion:

$$S(n) \geq S(n-2) + 5$$

which gives us the claimed lower bound on the edge-set size of the FS. To prove that the bound is indeed tight, we use the graph shown in Fig. 12. \square

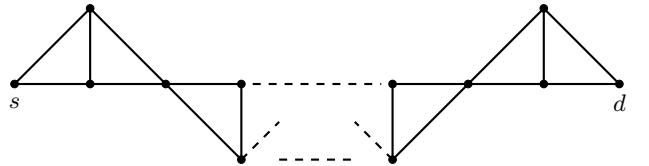


Figure 12: A graph that achieves the lower bound on the size of the FS for unweighted graphs.